

# *Chapter 3. Morphology and Finite-State Transducers*

From: Chapter 3 of *An Introduction to Natural Language Processing, Computational Linguistics, and Speech Recognition*, by Daniel Jurafsky and James H. Martin

# Background

- The problem of recognizing that *foxes* breaks down into the two morphemes *fox* and *-es* is called *morphological parsing*.
- Similar problem in the information retrieval domain: *stemming*
- Given the **surface** or **input form** *going*, we might want to produce the parsed form: VERB-go + GERUND-ing
- In this chapter
  - morphological knowledge and
  - The **finite-state transducer**
- It is quite inefficient to list all forms of noun and verb in the dictionary because the productivity of the forms.
- Morphological parsing is necessary more than just IR, but also
  - Machine translation
  - Spelling checking

# Survey of (Mostly) English Morphology

- Morphology is the study of the way words are built up from smaller meaning-bearing units, **morphemes**.
- Two broad classes of morphemes:
  - **The stems:** the “main” morpheme of the word, supplying the main meaning, while
  - **The affixes:** add “additional” meaning of various kinds.
- Affixes are further divided into **prefixes, suffixes, infixes, and circumfixes**.
  - Suffix: *eat-s*
  - Prefix: *un-buckle*
  - Circumfix: *ge-sag-t* (said) *sagen* (to say) (in German)
  - Infix: *hingi* (borrow) *humingi* (the agent of an action) (in Philippine language Tagalog)

# Survey of (Mostly) English Morphology

- Prefixes and suffixes are often called **concatenative morphology**.
- A number of languages have extensive **non-concatenative morphology**
  - The Tagalog infixation example
  - **Templatic morphology** or **root-and-pattern morphology**, common in Arabic, Hebrew, and other Semitic languages
- Two broad classes of ways to form words from morphemes:
  - **Inflection**: the combination of a word stem with a grammatical morpheme, usually resulting in a word of the same class as the original stem, and usually filling some syntactic function like agreement, and
  - **Derivation**: the combination of a word stem with a grammatical morpheme, usually resulting in a word of a *different* class, often with a meaning hard to predict exactly.

# Survey of (Mostly) English Morphology

## Inflectional Morphology

- In English, only nouns, verbs, and sometimes adjectives can be inflected, and the number of affixes is quite small.
- Inflections of nouns in English:
  - An affix marking **plural**,
    - cat(-s), thrush(-es), ox (oxen), mouse (mice)
    - ibis(-es), waltz(-es), finch(-es), box(-es), butterfly(-lies)
  - An affix marking **possessive**
    - llama's, children's, llamas', Euripides' comedies

# Survey of (Mostly) English Morphology

## Inflectional Morphology

- Verbal inflection is more complicated than nominal inflection.
  - English has three kinds of verbs:
    - **Main verbs**, *eat, sleep, impeach*
    - **Modal verbs**, *can will, should*
    - **Primary verbs**, *be, have, do*
  - Morphological forms of regular verbs

stem	walk	merge	try	map
-s form	walks	merges	tries	maps
-ing principle	walking	merging	trying	mapping
Past form or <i>-ed</i> participle	walked	merged	tried	mapped

- These regular verbs and forms are significant in the morphology of English because of their *majority* and being *productive*.

# Survey of (Mostly) English Morphology

## Inflectional Morphology

- Morphological forms of irregular verbs

stem	eat	catch	cut
-s form	eats	catches	cuts
-ing principle	eating	catching	cutting
Past form	ate	caught	cut
-ed participle	eaten	caught	cut

# Survey of (Mostly) English Morphology

## Derivational Morphology

- **Nominalization** in English:
  - The formation of new nouns, often from verbs or adjectives

Suffix	Base Verb/Adjective	Derived Noun
-action	computerize (V)	computerization
-ee	appoint (V)	appointee
-er	kill (V)	killer
-ness	fuzzy (A)	fuzziness

- Adjectives derived from nouns or verbs

Suffix	Base Noun/Verb	Derived Adjective
-al	computation (N)	computational
-able	embrace (V)	embraceable
-less	clue (A)	clueless



# Survey of (Mostly) English Morphology

## Derivational Morphology

- Derivation in English is more complex than inflection because
  - Generally less productive
    - A nominalizing affix like *-ation* can not be added to absolutely every verb.  
*eatation*(\*)
  - There are subtle and complex meaning differences among nominalizing suffixes. For example, *sincerity* has a subtle difference in meaning from *sincereness*.

# Finite-State Morphological Parsing

- Parsing English morphology

<b>Input</b>	<b>Morphological parsed output</b>
cats	cat +N +PL
cat	cat +N +SG
cities	city +N +PL
geese	goose +N +PL
goose	(goose +N +SG) or (goose +V)
gooses	goose +V +3SG
merging	merge +V +PRES-PART
caught	(caught +V +PAST-PART) or (catch +V +PAST)

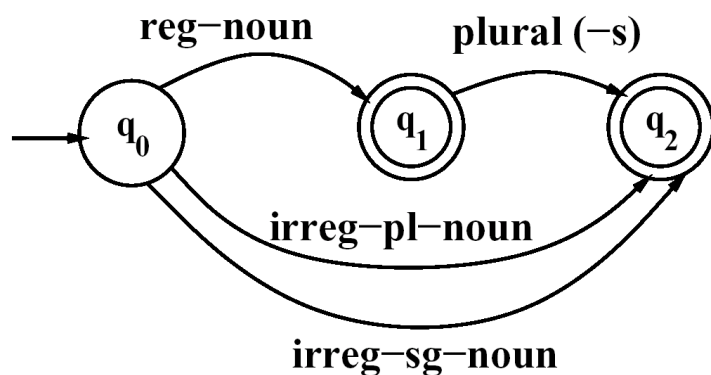
# Finite-State Morphological Parsing

- We need at least the following to build a morphological parser:
  1. **Lexicon**: the list of stems and affixes, together with basic information about them (Noun stem or Verb stem, etc.)
  2. **Morphotactics**: the model of morpheme ordering that explains which classes of morphemes can follow other classes of morphemes inside a word. E.g., the rule that English plural morpheme follows the noun rather than preceding it.
  3. **Orthographic rules**: these **spelling rules** are used to model the changes that occur in a word, usually when two morphemes combine (e.g., the  $y \rightarrow ie$  spelling rule changes *city* + *-s* to *cities*).

# Finite-State Morphological Parsing

## The Lexicon and Morphotactics

- A lexicon is a repository for words.
  - The simplest one would consist of an explicit list of every word of the language.  
*Inconvenient or impossible!*
  - Computational lexicons are usually structured with
    - a list of each of the stems and
    - Affixes of the language together with a representation of morphotactics telling us how they can fit together.
  - The most common way of modeling morphotactics is the finite-state automaton.

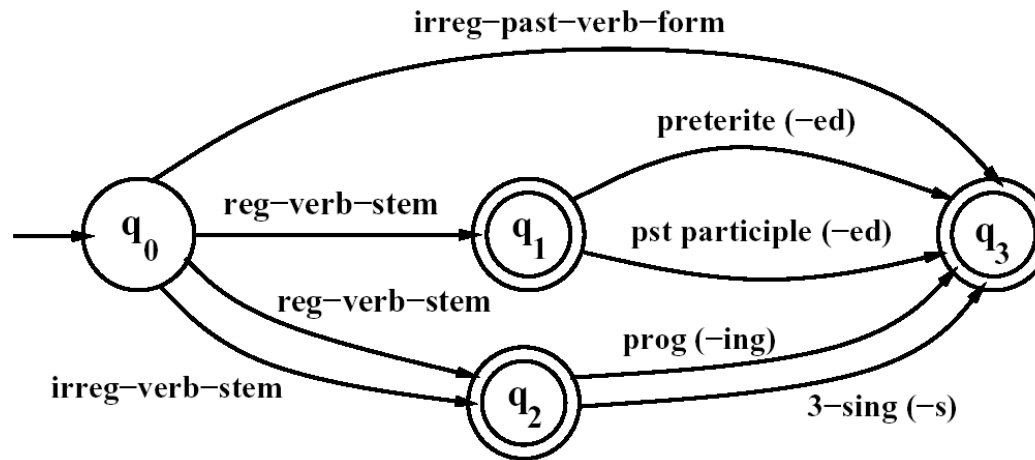


*An FSA for English nominal inflection*

Reg-noun	Irreg-pl-noun	Irreg-sg-noun	plural
fox	geese	goose	-s
fat	sheep	sheep	
fog	Mice	mouse	
fardvark			

# Finite-State Morphological Parsing

## The Lexicon and Morphotactics



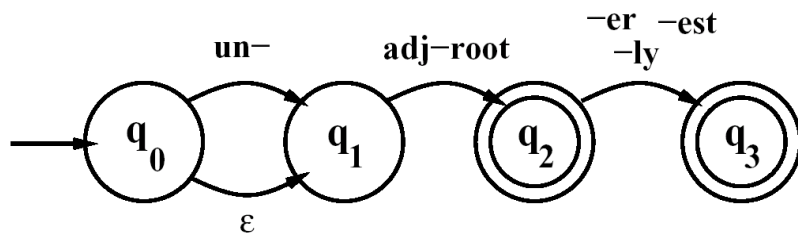
*An FSA for English verbal inflection*

Reg-verb-stem	Irreg-verb-stem	Irreg-past-verb	past	Past-part	Pres-part	3sg
walk	cut	caught	-ed	-ed	-ing	-s
fry	speak	ate				
talk	sing	eaten				
impeach	sang					
	spoken					

# Finite-State Morphological Parsing

## The Lexicon and Morphotactics

- English derivational morphology is more complex than English inflectional morphology, and so automata of modeling English derivation tends to be quite complex.
  - Some even based on CFG
- A small part of morphosyntactics of English adjectives

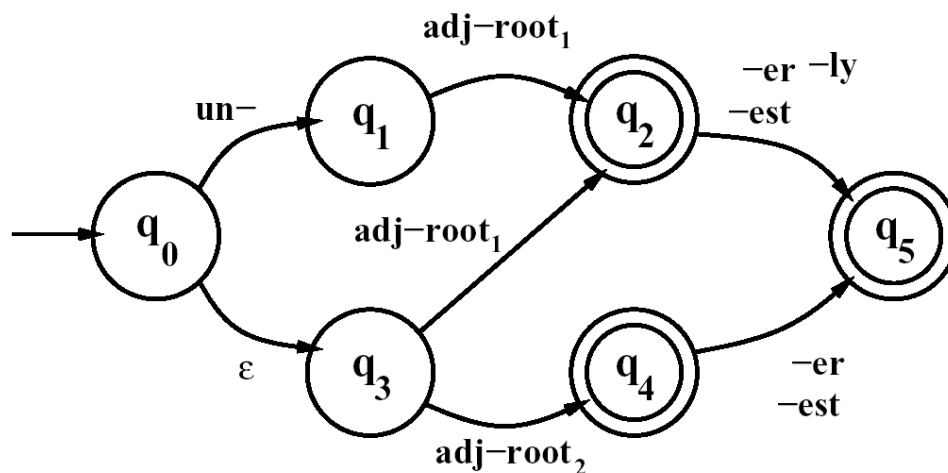


*An FSA for a fragment of English adjective Morphology #1*

big, bigger, biggest  
cool, cooler, coolest, coolly  
red, redder, reddest  
clear, clearer, clearest, clearly, unclear, unclearly  
happy, happier, happiest, happily  
unhappy, unhappier, unhappiest, unhappily  
real, unreal, really

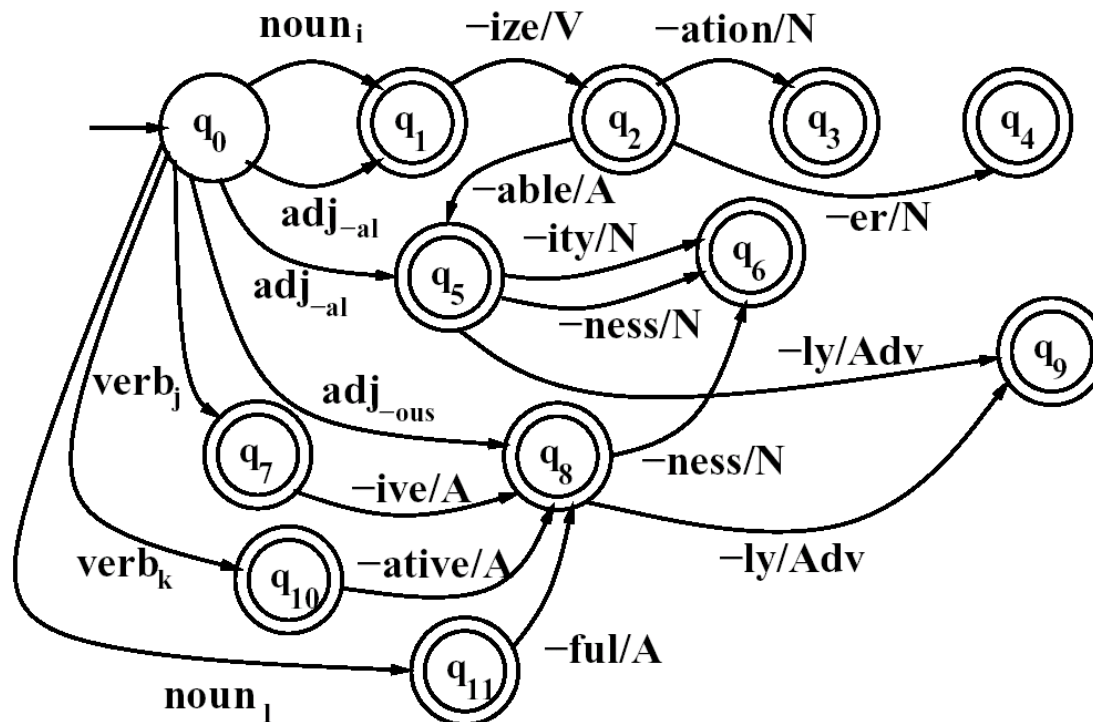
# Finite-State Morphological Parsing

- The FSA#1 recognizes all the listed adjectives, and ungrammatical forms like *unbig*, *redly*, and *realest*.
- Thus #1 is revised to become #2.
- The complexity is expected from English derivation.



*An FSA for a fragment of English adjective Morphology #2*

# Finite-State Morphological Parsing

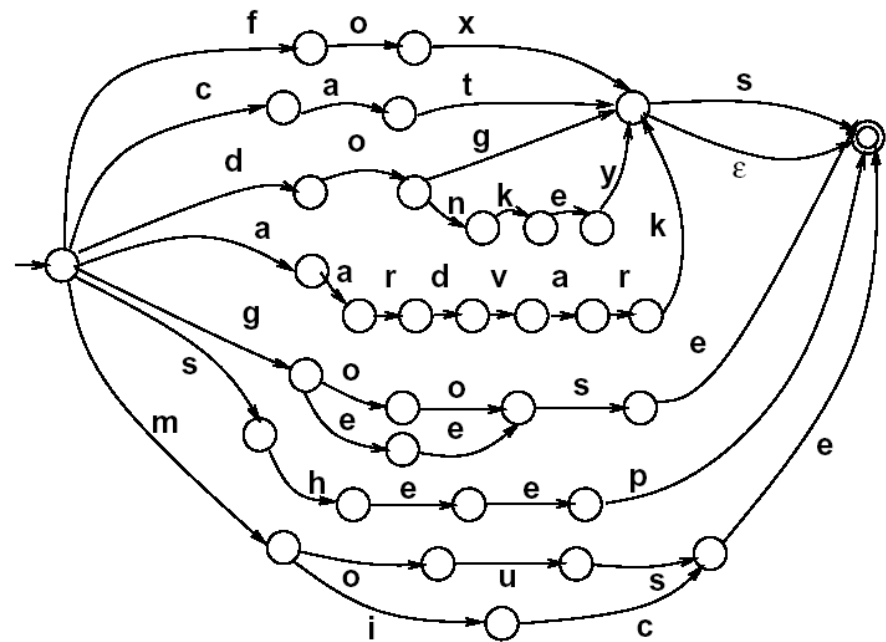


*An FSA for another fragment of English derivational morphology*



# Finite-State Morphological Parsing

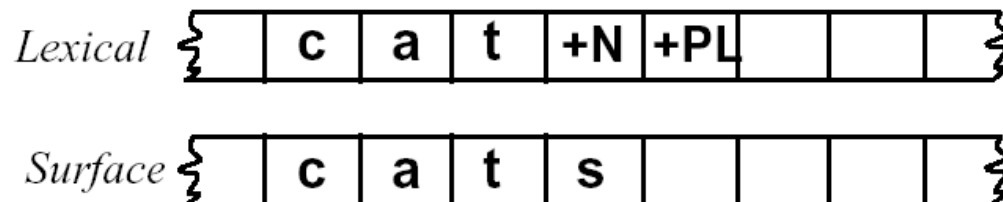
- We can now use these FSAs to solve the problem of **morphological recognition**:
  - Determining whether an input string of letters makes up a legitimate English word or not
  - We do this by taking the morphotactic FSAs, and plugging in each “sub-lexicon” into the FSA.
  - The resulting FSA can then be defined as the level of the individual letter.



# Finite-State Morphological Parsing

## Morphological Parsing with FST

- Given the input, for example, *cats*, we would like to produce *cat +N +PL*.
- Two-level morphology, by Koskenniemi (1983)
  - Representing a word as a correspondence between a **lexical level**
    - Representing a simple concatenation of morphemes making up a word, and
  - The **surface level**
    - Representing the actual spelling of the final word.
- Morphological parsing is implemented by building mapping rules that maps letter sequences like *cats* on the surface level into morpheme and features sequence like *cat +N +PL* on the lexical level.



# Finite-State Morphological Parsing

## Morphological Parsing with FST

- The automaton we use for performing the mapping between these two levels is the **finite-state transducer** or **FST**.
  - A transducer maps between one set of symbols and another;
  - An FST does this via a finite automaton.
- Thus an FST can be seen as a two-tape automaton which **recognizes** or **generates *pairs*** of strings.
- The FST has a more general function than an FSA:
  - An FSA defines a formal language
  - An FST defines a relation between sets of strings.
- Another view of an FST:
  - A machine reads one string and generates another.

# Finite-State Morphological Parsing

## Morphological Parsing with FST

- **FST as recognizer:**
  - a transducer that takes a pair of strings as input and output *accept* if the string-pair is in the string-pair language, and a *reject* if it is not.
- **FST as generator:**
  - a machine that outputs pairs of strings of the language. Thus the output is a yes or no, and a pair of output strings.
- **FST as transducer:**
  - A machine that reads a string and outputs another string.
- **FST as set relater:**
  - A machine that computes relation between sets.

# Finite-State Morphological Parsing

## Morphological Parsing with FST

- A formal definition of FST (based on the **Mealy machine** extension to a simple FSA):
  - $Q$ : a finite set of  $N$  states  $q_0, q_1, \dots, q_N$
  - $\Sigma$ : a finite alphabet of complex symbols. Each complex symbol is composed of an input-output pair  $i : o$ ; one symbol  $I$  from an input alphabet  $I$ , and one symbol  $o$  from an output alphabet  $O$ , thus  $\Sigma \subseteq I \times O$ .  $I$  and  $O$  may each also include the epsilon symbol  $\epsilon$ .
  - $q_0$ : the start state
  - $F$ : the set of final states,  $F \subseteq Q$
  - $\delta(q, i:o)$ : the transition function or transition matrix between states. Given a state  $q \in Q$  and complex symbol  $i:o \in \Sigma$ ,  $\delta(q, i:o)$  returns a new state  $q' \in Q$ .  $\delta$  is thus a relation from  $Q \times \Sigma$  to  $Q$ .

# Finite-State Morphological Parsing

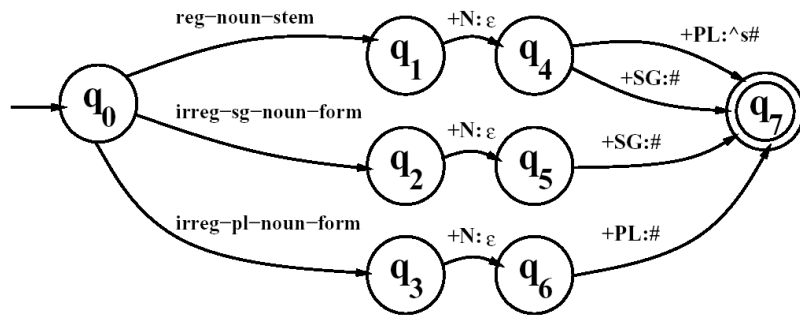
## Morphological Parsing with FST

- FSAs are isomorphic to regular languages, FSTs are isomorphic to **regular relations**.
- Regular relations are sets of pairs of strings, a natural extension of the regular language, which are sets of strings.
- FSTs are closed under union, but generally they are not closed under difference, complementation, and intersection.
- Two useful closure properties of FSTs:
  - **Inversion:** If  $T$  maps from  $I$  to  $O$ , then the inverse of  $T$ ,  $T^{-1}$  maps from  $O$  to  $I$ .
  - **Composition:** If  $T_1$  is a transducer from  $I_1$  to  $O_1$  and  $T_2$  a transducer from  $I_2$  to  $O_2$ , then  $T_1 \circ T_2$  maps from  $I_1$  to  $O_2$

# Finite-State Morphological Parsing

## Morphological Parsing with FST

- Inversion is useful because it makes it easy to convert a FST-as-parser into an FST-as-generator.
- Composition is useful because it allows us to take two transducers than run in series and replace them with one complex transducer.
  - $T_1 \circ T_2(S) = T_2(T_1(S))$

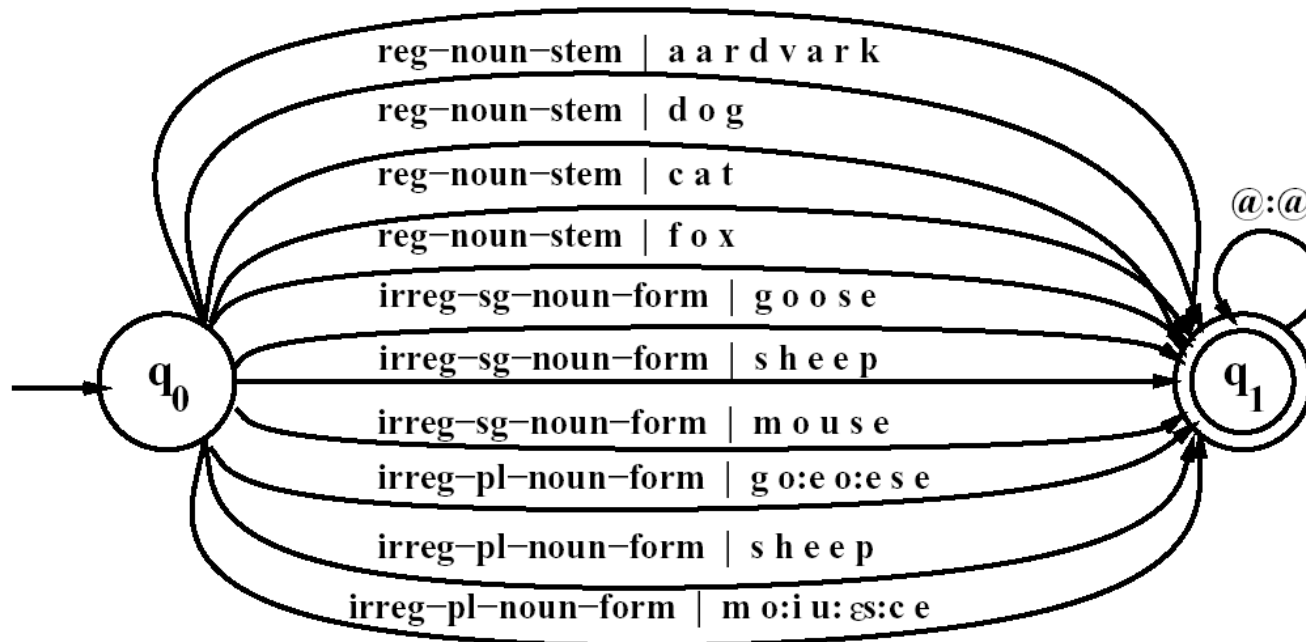


*A transducer for English nominal number inflection  $T_{num}$*

Reg-noun	Irreg-pl-noun	Irreg-sg-noun
fox	g o:e o:e s e	goose
fat	sheep	sheep
fog	m o:i u:es:c e	mouse
aardvark		

# Finite-State Morphological Parsing

## Morphological Parsing with FST

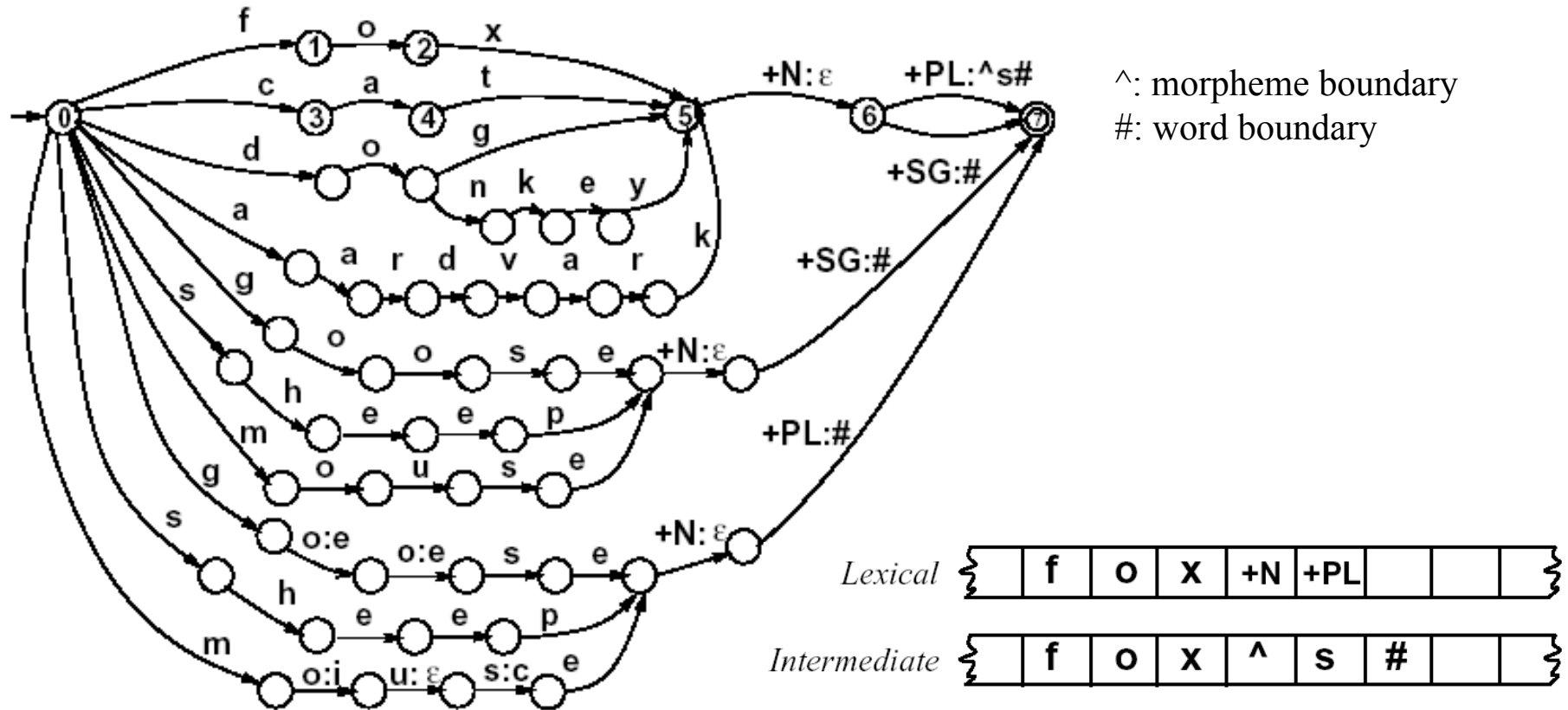


*The transducer  $T_{stems}$ , which maps roots to their root-class*



# Finite-State Morphological Parsing

## Morphological Parsing with FST



*A fleshed-out English nominal inflection FST*

$$T_{lex} = T_{num} \circ T_{stems}$$

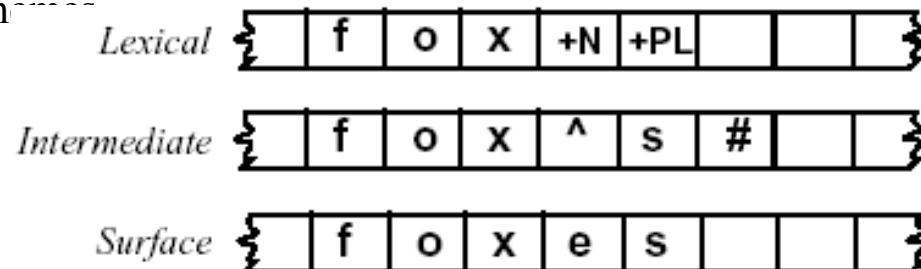
# Finite-State Morphological Parsing

## Orthographic Rules and FSTs

- **Spelling rules (or orthographic rules)**

Name	Description of Rule	Example
Consonant doubling	1-letter consonant doubled before <i>-ing/-ed</i>	beg/begging
E deletion	Silent e dropped before <i>-ing</i> and <i>-ed</i>	make/making
E insertion	e added after <i>-s, -z, -x, -ch, -sh</i> , before <i>-s</i>	watch/watches
Y replacement	<i>-y</i> changes to <i>-ie</i> before <i>-s, -i</i> before <i>-ed</i>	try/tries
K insertion	Verb ending with <i>vowel + -c</i> add <i>-k</i>	panic/panicked

- These spelling changes can be thought as taking as input a simple concatenation of morphemes and producing as output a slightly-modified concatenation of morphemes



# Finite-State Morphological Parsing

## Orthographic Rules and FSTs

- “insert an  $e$  on the surface tape just when the lexical tape has a morpheme ending in  $x$  (or  $z$ , etc) and the next morphemes is  $-s$ ”

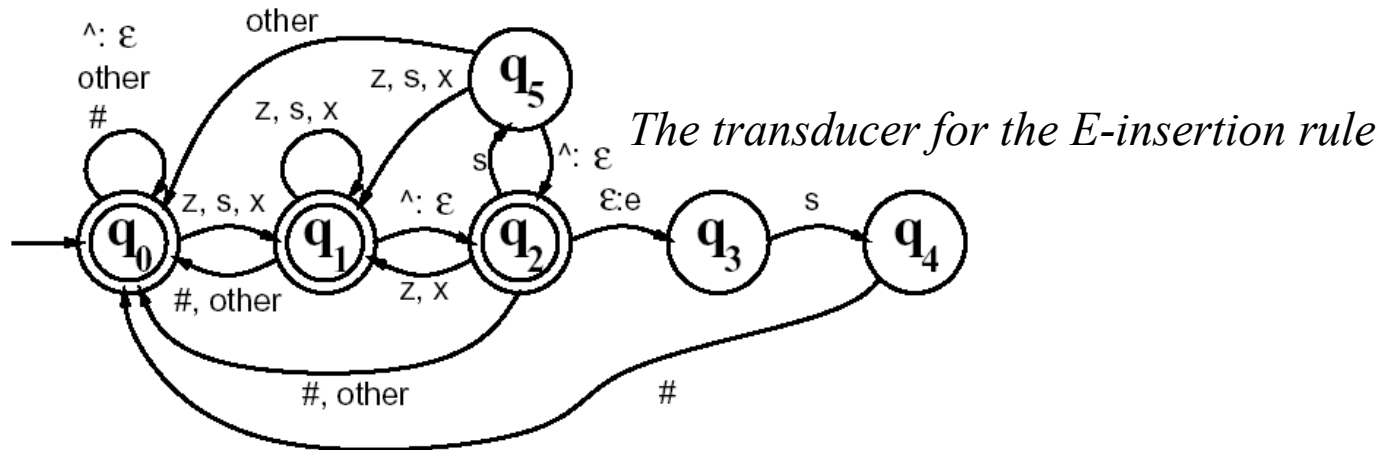
$$\varepsilon \rightarrow e / \left\{ \begin{array}{c} x \\ s \\ z \end{array} \right\} \_ s\#$$

- “rewrite  $a$  to  $b$  when it occurs between  $c$  and  $d$ ”

$$a \rightarrow b / c \_ d$$

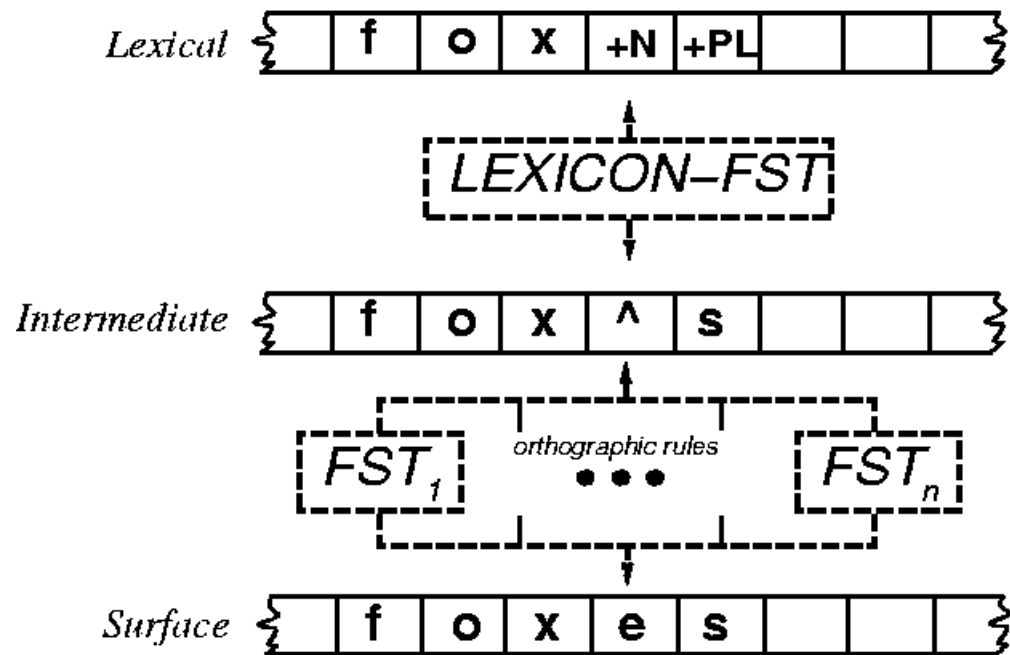
# Finite-State Morphological Parsing

## Orthographic Rules and FSTs



State \ Input	s : s	x : x	z : z	^ : ε	ε : e	#	other
$q_0$ :	1	1	1	0	-	0	0
$q_1$ :	1	1	1	2	-	0	0
$q_2$ :	5	1	1	0	3	0	0
$q_3$ :	4	-	-	-	-	-	-
$q_4$ :	-	-	-	-	-	0	-
$q_5$ :	1	1	1	2	-	-	0

# Combining FST Lexicon and Rules





# Combining FST Lexicon and Rules

- The power of FSTs is that the exact same cascade with the same state sequences is used
  - when machine is generating the surface form from the lexical tape, or
  - When it is parsing the lexical tape from the surface tape.
- Parsing can be slightly more complicated than generation, because of the problem of **ambiguity**.
  - For example, *foxes* could be  $f \circ x \ +V \ +3SG$  as well as  $f \circ x \ +N \ +PL$

# Lexicon-Free FSTs: the Porter Stemmer

- Information retrieval
- One of the mostly widely used **stemming** algorithms is the simple and efficient Porter (1980) algorithm, which is based on a series of simple cascaded rewrite rules.
  - ATIONAL → ATE (e.g., relational → relate)
  - ING → εif stem contains vowel (e.g., motoring → motor)
- Problem:
  - Not perfect: error of commision, omission
- Experiments have been made
  - Some improvement with smaller documents
  - Any improvement is quite small